## Chapter 6: SOLVING QUADRATIC EQUATIONS

A quadratic equation has the form $a x^{2}+b x+c=0$.
There are two methods that are commonly used for solving quadratic equations:

* factorising
* the quadratic formula

Note that not all quadratic equations can be solved by factorising. The quadratic formula can always be used however.

## Method 1: Factorising

Make sure that the equation is rearranged so that the right hand side is 0 . It usually makes it easier if the coefficient of $x^{2}$ is positive.

Example 1: Solve $x^{2}-3 x+2=0$
Factorise $\quad(x-1)(x-2)=0$
Either $(x-1)=0$ or $(x-2)=0$
So the solutions are $x=1$ or $x=2$
Note: The individual values $x=1$ and $x=2$ are called the roots of the equation.

Example 2: Solve $x^{2}-2 x=0$
Factorise: $\quad x(x-2)=0$
Either $x=0$ or $(x-2)=0$
So $x=0$ or $x=2$

## Method 2: Using the formula

Recall that the roots of the quadratic equation $a x^{2}+b x+c=0$ are given by the formula:

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$

Example 3: Solve the equation $2 x^{2}-5=7-3 x$
Solution: First we rearrange so that the right hand side is 0 . We get $2 x^{2}+3 x-12=0$
We can then tell that $a=2, b=3$ and $c=-12$.
Substituting these into the quadratic formula gives:

$$
x=\frac{-3 \pm \sqrt{3^{2}-4 \times 2 \times(-12)}}{2 \times 2}=\frac{-3 \pm \sqrt{105}}{4} \quad \text { (this is the surd form for the solutions) }
$$

If we have a calculator, we can evaluate these roots to get: $x=1.81$ or $x=-3.31$
If you need more help with the work in this chapter, there is an information booklet downloadable from this web site:
http://www.mathcentre.ac.uk/resources/workbooks/mathcentre/web-quadraticequations.pdf

## EXERCISE

1) Use factorisation to solve the following equations:
a) $x^{2}+3 x+2=0$
b) $x^{2}-3 x-4=0$
c) $x^{2}=15-2 x$
2) Find the roots of the following equations:
a) $x^{2}+3 x=0$
b) $x^{2}-4 x=0$
c) $\quad 4-x^{2}=0$
3) Solve the following equations either by factorising or by using the formula:
a) $6 x^{2}-5 x-4=0$
b) $8 x^{2}-24 x+10=0$
4) Use the formula to solve the following equations to 3 significant figures. Some of the equations can't be solved.
a) $x^{2}+7 x+9=0$
b) $6+3 x=8 x^{2}$
c) $4 x^{2}-x-7=0$
d) $x^{2}-3 x+18=0$
e) $3 x^{2}+4 x+4=0$
f) $3 x^{2}=13 x-16$
